# Competing Teams

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## Introduction

- Firms often compete in output markets that are not competitive
  - Patent race between pharmaceuticals (winner-takes-all)
  - Positive knowledge spillovers from copying technology
  - Market Power and oligopoly
  - ...
- Externalities affect effort provision (tournaments, contests,...)
- But also: how firms choose skill composition
  - Pharmaceutical with best scientists is more likely to get patent
  - Firms spend time and resources picking best team (including poaching from competitors)
  - ..

# THE PROBLEM

- We analyze assortative matching with externalities
  - · Standard model: match output depends only on matched pair
  - Here: match output depends also on other pairs
- Natural extension of Becker (1973)
  - 1. The output market is non-competitive
  - 2. The input/labor market is competitive
- Issues of interest:
  - Optimal versus equilibrium matching
  - Given output market: welfare improving intervention in input market
- Applications
  - 1. Knowledge Spillovers and within/between firm inequality
  - 2. Oligopoly
  - 3. Policy and Sports Competitions

# Take Away

- 1. Multiple equilibria
- 2. Interior equilibrium and planner's solution: mixed matching
- 3. Complementarity is not sufficient for PAM
- 4. Inefficiency: equilibrium vs. planner's allocation discontinuous
- 5. Applications: rationale evolution within- and between-firm inequality

#### Overview of the model

- Large number of heterogeneous workers (and firms)
- Two stages:
  - 1. Matching: Workers form teams of size 2 (competitive labor market)
  - 2. Competition: Teams compete in output market (incomplete markets)
- Second stage: match payoff depends on composition of competitor(s)
  - 1. Aggregate Spillovers: endogenous growth (copying)
  - 2. Pairwise Assignment with Local Spillovers
    - A Random Pairwise Assignment: sports competitions
    - B Deterministic Pairwise Assignment: oligopoly
    - C Directed Pairwise Assignment: internalize externality
- First stage: Analysis of sorting patterns
  - Planner vs. Competitive Equilibrium
  - Wedge between two outcomes due to externalities

- Continuum of agents
  - 1. Binary Types
    - Each has a 'type'  $x \in \{\underline{x}, \overline{x}\}$ ,  $\overline{x} > \underline{x}$  (equal measure)
    - Workers form teams of size 2  $\overline{X} = \{\overline{x}, \overline{x}\}$  or  $\hat{X} = \{\overline{x}, \underline{x}\}$  with  $\underline{X} < \hat{X} < \overline{X}$
  - 2. Continuum of types x
- Transferable utility
- Matching  $\mu$  partitions population in pairs:
  - PAM  $\mu_+$  binary: half of the teams are  $\overline{X}$  and half  $\underline{X}$
  - NAM  $\mu_-$  binary: all the teams are  $\hat{X}$
  - Mixed  $\mu(\alpha)$ : fraction  $\frac{\alpha}{2}$  are  $\overline{X}, \underline{X}$ ; fraction  $1 \alpha$  are  $\hat{X}$

- Aggregate externality:  $\mathcal{V}(X|\mu)$
- Pairwise assignment: Teams compete pairwise in downstream interaction (e.g., output market) against a randomly drawn team
  - $V(X_i|X_j)$ : match output of team  $X_i$  when competing with  $X_j$
  - With Random Assignment

$$\mathcal{V}(X_i|\mu_+) = \mathbb{E}_{\mu_+}[V(X_i|\tilde{X}_j)] = \frac{1}{2}V(X_i|\overline{X}) + \frac{1}{2}V(X_i|\underline{X})$$
$$\mathcal{V}(X_i|\mu_-) = \mathbb{E}_{\mu_-}[V(X_i|\tilde{X}_j)] = V(X_i|\hat{X})$$

• Gradually, provide micro foundations for  $\mathcal{V}(X|\mu) \to V(X_i|X_i) \to ...$ 

#### An example - Patent Race

- Research: uncertainty about the exact outcome  $v_i$ 
  - 1. Form R&D teams
  - 2. Draw uncertain research output  $v_i$ :
    - $v_i \in \{0, v\}$
    - probability of v given team  $X_i$ :  $p_i = p(X_i)$  (with  $\overline{p} > \hat{p} > p$ )
  - 3. Winner takes all:  $\max\{v_i, v_i\}$  (half in case of a tie)
- Expected payoff:

$$V(X_i|X_j) = p_i p_j \frac{v}{2} + p_i (1 - p_j) v = v p_i - \frac{v}{2} p_i p_j$$

$$\Rightarrow$$
 e.g.  $V(\overline{X}|\underline{X}) = v\overline{p} - \frac{v}{2}\overline{p}\underline{p}$  and  $V(\overline{X}|\overline{X}) = v\overline{p} - \frac{v}{2}\overline{p}\underline{p}$ 

$$\Rightarrow \quad \mathcal{V}(\overline{X}|\mu_{+}) = \frac{1}{2} \left( v \overline{p} - \frac{v}{2} \overline{p} \underline{p} \right) + \frac{1}{2} \left( v \overline{p} - \frac{v}{2} \overline{p}^{2} \right)$$

# SOLUTION

**Planner:** Takes as given output market competition and chooses  $\mu$  that maximizes sum of teams' outputs

• PAM optimal if

$$\mathcal{V}(\overline{X}|\mu_{+}) + \mathcal{V}(\underline{X}|\mu_{+}) \ge 2\mathcal{V}(\hat{X}|\mu_{-})$$

• NAM optimal if

$$\mathcal{V}(\overline{X}|\mu_+) + \mathcal{V}(\underline{X}|\mu_+) \le 2\mathcal{V}(\hat{X}|\mu_-)$$

Reduces to supermodularity (or submodularity) without externalities

$$\mathcal{V}(\overline{X}) + \mathcal{V}(\underline{X})$$
 vs.  $2\mathcal{V}(\hat{X})$ 

# SOLUTION

**Competitive Equilibrium:** Agents take market wages and matching as given when they choose partners

- $(\underline{w}, \overline{w}, \mu)$  such that (i) each type maximizes his payoff given wages; and (ii) choices are consistent with  $\mu$  (market clearing)
- PAM if

$$\mathcal{V}(\overline{X}|\mu_{+}) - \overline{w} \geq \mathcal{V}(\hat{X}|\mu_{+}) - \underline{w}$$
$$\mathcal{V}(\underline{X}|\mu_{+}) - \underline{w} \geq \mathcal{V}(\hat{X}|\mu_{+}) - \overline{w}$$

 $\Rightarrow \mathcal{V}(\cdot|\mu_+)$  supermodular, or

$$\mathcal{V}(\overline{X}|\mu_+) + \mathcal{V}(\underline{X}|\mu_+) \ge 2\mathcal{V}(\hat{X}|\mu_+)$$

• Wages:  $\overline{w}=\frac{1}{2}\mathcal{V}(\overline{X}|\mu_+)$  and  $\underline{w}=\frac{1}{2}\mathcal{V}(\underline{X}|\mu_+)$ 

## RESULTS

- Let  $\frac{\alpha}{2}$  be fraction of  $\overline{X}$ ,  $\underline{X}$  teams, and  $(1-\alpha)$  fraction of  $\hat{X}$  teams
- Define

$$\Gamma(\alpha) = \mathcal{V}(\overline{X}|\alpha) + \mathcal{V}(\underline{X}|\alpha) - 2\mathcal{V}(\hat{X}|\alpha),$$

This function is linear in  $\alpha$ , so is  $\mathcal{V}(X|\alpha)$ 

$$\mathcal{V}(X|\alpha) = \alpha \mathcal{V}(X|1) + (1-\alpha)\mathcal{V}(X|0)$$

This implies

$$\Gamma(\alpha) = \alpha \Gamma(1) + (1 - \alpha) \Gamma(0)$$

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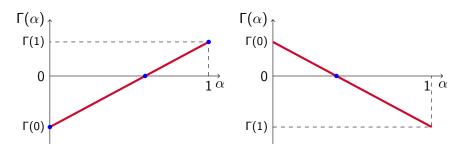
$$\Gamma(\alpha) = \alpha \Gamma(1) + (1 - \alpha) \Gamma(0)$$

### **PROPOSITION**

A competitive equilibrium exists. It exhibits PAM if  $\Gamma(1) \geq 0$ , NAM if  $\Gamma(0) \leq 0$ , and it is interior with  $0 < \alpha < 1$  if  $\Gamma(\alpha) = 0$ .

# RESULTS

- Unlike Becker, without externalities
  - 1. There can be interior equilibria  $\alpha \in (0,1)$
  - 2. There can be multiple equilibria



### Results – Planner

Planner's solution can be interior:

$$\max_{\alpha \in [0,1]} \qquad \frac{1}{2} \left( \frac{\alpha}{2} \mathcal{V}(\overline{X}|\alpha) + \frac{\alpha}{2} \mathcal{V}(\underline{X}|\alpha) + (1-\alpha) \mathcal{V}(\hat{X}|\alpha) \right)$$

or equivalently

$$\max_{\alpha \in [0,1]} \frac{1}{2} \left( \frac{\alpha^2}{2} A + \frac{\alpha}{2} B + C \right)$$

$$(0) R = \Gamma(0) + 2(2(\hat{\mathbf{Y}}|1) - 2(\hat{\mathbf{Y}}|0)) C = 2(\hat{\mathbf{Y}}|0)$$

where 
$$A \equiv \Gamma(1) - \Gamma(0)$$
,  $B \equiv \Gamma(0) + 2(\mathcal{V}(\hat{X}|1) - \mathcal{V}(\hat{X}|0))$ ,  $C \equiv \mathcal{V}(\hat{X}|0)$ 

• Quadratic objective: convex ⇒ corner; concave ⇒ interior or corner

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• Quadratic objective: convex  $\Rightarrow$  corner; concave  $\Rightarrow$  interior or corner

### **PROPOSITION**

Assume that either  $A \neq 0$  or  $B \neq 0$ . The optimal matching  $\alpha^p$  is as follows: (i) If  $A \geq 0$ , then  $\alpha^p = 1$  if  $A + B \geq 0$  and  $\alpha^p = 0$  if A + B < 0;

(ii) If 
$$A < 0$$
 and  $B < 0$ , then  $\alpha^p = 0$ :

(iii) If 
$$A < 0$$
,  $B > 0$ , and  $B + 2A \ge 0$ , then  $\alpha^p = 1$ ;

(iv) If 
$$A < 0$$
,  $B > 0$ , and  $B + 2A < 0$ , then  $\alpha^p = -B/2A \in (0,1)$ .

# SORTING AND INEFFICIENCY

### PROPOSITION

There is an equilibrium with PAM allocation while there is NAM in the planner's solution if and only if

(i)  $V(X|\mu_+)$  supermodular in X;

$$(ii) \ \mathcal{V}(\overline{X}|\mu_{+}) + \mathcal{V}(\underline{X}|\mu_{+}) - 2\mathcal{V}(\hat{X}|\mu_{+}) \leq 2[\mathcal{V}(\hat{X}|\mu_{-}) - \mathcal{V}(\hat{X}|\mu_{+})]$$

- Intuition:
  - "Supermodularity" (modified)
  - Differential externality NAM outweighs "supermodularity"
- Similar conditions for NAM equilibrium, PAM planner

# SORTING AND INEFFICIENCY

#### Special Cases

# 1. Additively Separable Payoffs

- $\mathcal{V}(X_i|\mu) = g(X_i) + h(\mu)$
- $h(\mu_+) = \frac{1}{2}h(\overline{X}) + \frac{1}{2}h(\underline{X})$  and  $h(\mu_-) = h(\hat{X})$
- PAM equilibrium and NAM planner iff

g SPM and 
$$g(\overline{X}) + g(\underline{X}) - 2g(\hat{X}) \le 2[h(\mu_{-}) - h(\mu_{+})]$$

# SORTING AND INEFFICIENCY

#### Special Cases

# 1. Additively Separable Payoffs

- $\mathcal{V}(X_i|\mu) = g(X_i) + h(\mu)$
- $h(\mu_+) = \frac{1}{2}h(\overline{X}) + \frac{1}{2}h(\underline{X})$  and  $h(\mu_-) = h(\hat{X})$
- · PAM equilibrium and NAM planner iff

$$g$$
 SPM and  $g(\overline{X}) + g(\underline{X}) - 2g(\hat{X}) \le 2[h(\mu_{-}) - h(\mu_{+})]$ 

- 2. Multiplicatively Separable Payoffs
  - $\mathcal{V}(X_i|\mu) = g(X_i)h(\mu)$
  - PAM equilibrium and NAM planner iff

$$g$$
 SPM and  $g(\overline{X}) + g(\underline{X}) - 2g(\hat{X}) \le 2g(\hat{X}) \frac{h(\mu_-) - h(\mu_+)}{h(\mu_+)}$ 

Need h 'sufficiently submodular' in X

### UNCERTAINTY

- Many economic environments involve uncertainty
- Set up:
  - 1. Team composition  $X_i$ : labor market competition
  - 2. Team generates stochastic product  $v_i$ , from  $F(v_i|X_i)$
  - 3. Output market competition  $z(v_i, v_i)$
- Expected output  $X_i : V(X_i|X_j) = \int \int z(v_i, v_j) dF(v_i|X_i) dF(v_j|X_j)$

$$V(X_{i}|X_{j}) = \underbrace{z(\underline{v},\underline{v}) + \int \frac{\partial z(v_{i},\underline{v})}{\partial i} S_{i} dv_{i} + \int 2 \frac{\partial z(\underline{v},v_{j})}{\partial j} S_{i} dv_{j}}_{g(X_{i})} + \underbrace{\int \frac{\partial z(\underline{v},v_{j})}{\partial j} S_{j} dv_{j} + \underbrace{\int \int \frac{\partial^{2}z}{\partial i \partial j} S_{i} S_{j} dv_{i} dv_{j}}_{k(X_{i},X_{j})}$$

where  $S_i = S(v|X_i) = 1 - F(v|X_i)$  is the survival function

# ECONOMIC APPLICATIONS

- I Knowledge Spillovers
- **II** Oligopoly
- **III** Policy and Sports Competitions

#### COPYING AND THE EVOLUTION OF INEQUALITY

- Recent increase in inequality: between-firm inequality, not within-firm Card-Heinig-Kline (2013), Benguria (2015), Valchos e.a. (2015), Song e.a. (2016), Barth e.a. (2014)
- Model of knowledge spillovers (Romer-Lucas):
  - Type-dependent copying technology: Lucas-Moll (2014),
     Benhabib-Perla-Tonetti (2017), Eeckhout-Jovanovic (2002)
  - With an ex ante competitive matching stage
     ⇒ Interior matching allocation
- Effect of increase in complementarity between workers
  - $\Rightarrow$  Increase in fraction  $\alpha$  of PAM matches
- Consistent with facts: between-firm inequality ↑ (of skills and wages)

#### COPYING AND THE EVOLUTION OF INEQUALITY

- Two types  $\overline{x}, \underline{x}$ , equal measure.  $X = x_1 + x_2$ . Aggregate Spillover
- Stage 2: Firms choose investment k to solve:

$$V(X|\alpha) = \max_{k} \left( A(\lambda + H(k, X))k - \frac{k^2}{2X^{\gamma}} \right),$$

where  $H(\cdot)$  is the CDF of all k in the economy:

$$H(k,X) = 0 \quad \forall k,$$

$$H(k,\hat{X}) = \begin{cases} 1 - \frac{\alpha}{2} - (1 - \alpha) & \text{if } k \in [0, \overline{\kappa}) \\ 0 & \text{if } k \ge \overline{\kappa}, \end{cases}$$

$$H(k,\underline{X}) = \begin{cases} 1 - \frac{\alpha}{2} & \text{if } k \in [0, \hat{\kappa}) \\ 1 - \frac{\alpha}{2} - (1 - \alpha) & \text{if } k \in [\hat{\kappa}, \overline{\kappa}) \\ 0 & \text{if } k \ge \overline{\kappa}. \end{cases}$$

• Stage 1: competitive labor market:  $\frac{\alpha}{2}$  firms  $\overline{X}$  and  $\underline{X}$ ;  $1-\alpha$  firms  $\hat{X}$ 

#### COPYING AND THE EVOLUTION OF INEQUALITY

### **PROPOSITION**

If  $\lambda \geq 1$ ,  $1 \leq \gamma < \overline{\gamma}$ , and  $\underline{x}/\overline{x}$  is sufficiently small, then there is a unique competitive equilibrium, which is interior (i.e.,  $\alpha \in (0,1)$ ). Moreover, the equilibrium  $\alpha$  is strictly increasing in  $\gamma$ .

- Calculate optimal  $k^*$  and the resulting H(k)
- Construct:  $\Gamma(\alpha) = \mathcal{V}(\overline{X}|\alpha) + \mathcal{V}(\underline{X}|\alpha) 2\mathcal{V}(\hat{X}|\alpha)$
- Apply Proposition above on interior solution and uniqueness
- $\frac{\partial \alpha}{\partial \gamma} > 0$ : apply Implicit Function Thm to  $\Gamma(\alpha; \gamma) = 0$

#### COPYING AND THE EVOLUTION OF INEQUALITY

• Within firm variance across all firms:  $Var[w|\alpha^*]$ 

$$ightarrow rac{\partial \mathsf{Var}[w|lpha^{\star}]}{\partial \gamma} pprox 0$$

• Between firm variance:  $Var[w_i + w_i | \alpha^*]$ 

$$\rightarrow \frac{\partial \mathsf{Var}[\mathit{w_i} + \mathit{w_j} | \alpha^\star]}{\partial \gamma} > 0$$

⇒ Increase in wage inequality: driven by between-firm variance; not within-firm variance

#### CONTINUUM OF TYPES

- Winner-takes-all: externality increasing in k
- · Objective: theoretical solution with continuum of types
- $x \sim U[0,1]; X = x_1 + x_2 (\gamma = 1)$
- Infinitely many matches, distributed G(X):
  - PAM:  $G(X) \sim U[0,2]$ , or  $G(X) = \frac{X}{2}$
  - NAM: all firms (x, 1 x) so X = 1 and G(X) mass point
- Stage 2 payoff function:

$$\mathcal{V}(X_i|\mu) = \max_{k_i} \left\{ AH(k_i, \mu)k_i - \frac{k_i^2}{2X_i} \right\}$$

• where  $H(\cdot)$  is the distribution of k. FOC:

$$A[H+k_iH']=\frac{k_i}{X_i}$$

• Consistency:  $H(k_i) = G(X_i)$ 

#### PLANNER - PAM

• Use  $H(k_i) = G(X_i) = X_i/2$  (under PAM) to solve for  $X_i$  in the FOC:

$$H(k_i) = \frac{k_i}{2A[H+k_iH']} \quad \Longleftrightarrow \quad H^2(k_i) + k_iH(k_i)H'(k_i) = \frac{k_i}{2A}.$$

• The solution to this differential equation is

$$H(k_i) \stackrel{c=0}{=} \sqrt{\frac{k_i}{3A}}$$
 and  $h(k_i) = \frac{1}{2\sqrt{3Ak_i}}$ ,

• Equilibrium investment  $k_i^* = \frac{3A}{4}X_i^2$  and payoff:

$$\mathcal{V}^{\star} = \frac{3}{32} A^2 X_i^3$$

Welfare:

$$W_{PAM} = \frac{3}{32}A^2 \int_0^2 X_i^3 d\frac{X_i}{2} = \frac{3}{16}A^2.$$

#### PLANNER - NAM

• Under NAM,  $G(X_i)$  has a mass point:

$$G(X_i) = \begin{cases} 0 & \text{if } x < 1; \\ 1 & \text{if } x \ge 1. \end{cases}$$

• Conjecture a symmetric equilibrium where:

$$V(X_i) = \begin{cases} Ak_i - \frac{k_i^2}{2X_i} & \text{if } k_i \ge k_{-i}; \\ -\frac{k_i^2}{2X_i} & \text{if } k_i < k_{-i}. \end{cases}$$

- NAM: continuum of allocations with  $k_i \in [A, 2A]$
- The Pareto optimal solution  $k^* = A$  with  $W_{NAM} = \frac{A^2}{2}$
- ⇒ Planner prefers Pareto optimal NAM over PAM

#### Competitive Equilibrium

• PAM provided  $\mathcal{V}^*(x_i + x_j | \mu) = \frac{3}{32} A^2 (x_i + x_j)^3$  supermodular in  $x_i, x_j$  or

$$\frac{\partial^2 \mathcal{V}^*(x_i + x_j | \mu)}{\partial x_i \partial x_j} = \frac{9}{16} A^2(x_i + x_j) > 0$$

Wages

$$w(x) = \int_0^x \frac{9}{32} A^2 (2s)^2 ds = \frac{3}{8} A^2 x^3$$

• NAM payoff  $V = \frac{A^2}{2(x_i + x_j)}$ : not an equilibrium because supermodular:

$$\frac{\partial^2 \mathcal{V}^*(x_i + x_j | \mu)}{\partial x_i \partial x_j} = \frac{A^2}{(x_i + x_j)^3} > 0$$

∴ PAM equilibrium; NAM Planner

# II. Oligopoly

- 2 firms; Linear demand  $p = a b(q_i + q_j)$ , with a > 0 and b > 0, where  $q_i$  and  $q_j$  are the outputs of the two firms.
- Cost  $C(x_k, x_k', q_k) = c(x_k, x_k')q_k$ ; cost-per-unit:  $c(x_k, x_k') = \nu \beta x_k x_k'$ , with  $\nu > \beta \overline{x}^2$ ,  $\beta > 0$ ; c is strictly submodular, that is,  $c_{12} = -\beta$ , with "degree" of submodularity indexed by  $\beta$ .
- To ensure interior solutions we will assume that  $a > 2c(\underline{x},\underline{x})$ .
- Nash equilibrium  $q_i = (a 2c(x_i, x_i') + c(x_j, x_j'))/(3b)$  with equilibrium price  $p = (a + c(x_i, x_i') + c(x_j, x_j'))/3$ . The profits:

$$V(x_{i}, x_{i}'|x_{j}, x_{j}') = \frac{(a - 2c(x_{i}, x_{i}') + c(x_{j}, x_{j}'))^{2}}{9b} = \frac{(a - 2(\nu - \beta x_{i}x_{i}') + \nu - \beta x_{j}x_{j}')^{2}}{9b}$$

$$V(x_{j}, x_{j}'|x_{i}, x_{i}') = \frac{(a - 2c(x_{j}, x_{j}') + c(x_{i}, x_{i}'))^{2}}{9b} = \frac{(a - 2(\nu - \beta x_{j}x_{j}') + \nu - \beta x_{i}x_{i}')^{2}}{9b}$$

# II. OLIGOPOLY

- MAtching PAM  $\mu_+(x) = x$ , ( $\eta$  is PAM too)
- Equilibrium wages are equal to

$$w(x) = w(\underline{x}) - \frac{4}{9b} \int_{\underline{x}}^{x} c_2(s, s)(a - c(s, s))ds$$

$$= w(\underline{x}) + \frac{4\beta}{9b} \int_{\underline{x}}^{x} s(a - \nu + \beta s^2)ds$$

$$= w(\underline{x}) + \frac{4\beta}{9b} \left( (a - \nu) \frac{x^2 - \underline{x}^2}{2} + \beta \frac{x^4 - \underline{x}^4}{4} \right),$$

# II. OLIGOPOLY

PAM equilibrium properties:

### PROPOSITION

If a is large enough, then there exists a competitive equilibrium with PAM. Wages increase in a and decrease in b, and firms with better composition of their labor force set higher markups.

• Variance is increasing in  $\beta$ , the degree of supermodularity  $\partial {\sf Var}(w)/\partial \beta > 0$ 

## III. POLICY AND SPORTS TEAMS

- Sports competitions: US vs. Europe
  - US: intervention for balanced competition: PAM → NAM
  - Europe: laissez-faire: PAM
- We use the model with negative spillovers  $z_i = v_0 + av_i + bv_i$
- Need to calculate wages
- Effects of policies:
  - 1. Taxes
    - Suitable taxes for hiring same type changes PAM to NAM
    - 2. Salary Cap
      - Bound on wage of high type cannot change PAM to NAM
    - 3. Rookie Draft
      - Senior types hire rookies
      - Sequential hiring at fixed type dependent wages: low senior types first
      - Equilibrium with NAM
      - Both senior types prefer it to PAM

### CONCLUSION

- Many output markets have externalities
- ⇒ How does it affect labor market? Assortative matching w/ externalities
  - Unlike standard (Becker) matching problem:
    - 1. Solution can be interior
    - 2. Multiple equilibria possible
    - 3. Allocation generically ineffecient
    - 4. If inefficient: drastic, discontinuous reallocation
  - Applications:
    - Knowledge spillovers: explain within/between-firm inequality
    - Oligopolistic output markets
    - Policy interventions

# Competing Teams

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